

### Log Properties 3 (GREEN)

Solve each equation. Pick 2 equations from each column to solve and do the rest for more practice.

1.  $\log_3(x+3) - \log_3(x+4) = 5$

$$\log_3 \frac{x+3}{x+4} = 5 \rightarrow 243(x+4) = x+3$$

$$243x + 972 = x+3$$

$$242x = -969$$

$$x = \frac{-969}{242}$$

$$3^5 = \frac{x+3}{x+4}$$

$$243 = \frac{x+3}{x+4}$$

5.  $\log_2(x) + \log_2(x+4) = 5$

$$\log_2 x(x+4) = 5 \rightarrow x^2 - 4x - 32 = 0$$

$$2^5 = x^2 + 4x$$

$$32 = x^2 + 4x$$

$$x^2 - 4x - 32 = 0$$

$$(x-4)(x+8) = 0$$

$$x = 4, -8$$

2.  $\log_7(x+2) - \log_7(x+3) = 4$

$$\log_7 \frac{x+2}{x+3} = 4 \rightarrow 2401(x+3) = x+2$$

$$2401x + 7203 = x+2$$

$$2400x = -7201$$

$$x = \frac{-7201}{2400}$$

$$7^4 = \frac{x+2}{x+3}$$

$$2401 = \frac{x+2}{x+3}$$

6.  $\log_3(x) + \log_3(x-2) = 8$

$$\log_3 x(x-2) = 8 \rightarrow x^2 - 2x - 6562 = 0$$

$$3^8 = x^2 - 2x$$

$$6562 = x^2 - 2x$$

$$x^2 - 2x - 6562 = 0$$

GF

$$x = -80.012, 82.012$$

3.  $\log_2(x-6) - \log_2(x+8) = 8$

$$\log_2 \frac{x-6}{x+8} = 8 \rightarrow 256(x+8) = x-6$$

$$256x + 2048 = x-6$$

$$255x = -2054$$

$$x = \frac{-2054}{255}$$

$$2^8 = \frac{x-6}{x+8}$$

$$256 = \frac{x-6}{x+8}$$

7.  $\log_4(x) + \log_4(x+5) = 2$

$$\log_4 x(x+5) = 2 \rightarrow x^2 + 5x - 16 = 0$$

$$4^2 = x^2 + 5x$$

$$16 = x^2 + 5x$$

$$x^2 + 5x - 16 = 0$$

GF

$$x = -7.217, 2.217$$

4.  $\log_4(x-4) - \log_4(x+7) = 9$

$$\log_4 \frac{x-4}{x+7} = 9 \rightarrow 262144(x+7) = x-4$$

$$262144x + 1835008 = x-4$$

$$262143x = -1835012$$

$$x = \frac{-1835012}{262143}$$

$$4^9 = \frac{x-4}{x+7}$$

$$262144 = \frac{x-4}{x+7}$$

8.  $\log_7(x) + \log_7(x-3) = 4$

$$\log_7 x(x-3) = 4 \rightarrow x^2 - 3x - 2401 = 0$$

$$7^4 = x^2 - 3x$$

$$2401 = x^2 - 3x$$

$$x^2 - 3x - 2401 = 0$$

GF

$$x = -47.523, 50.523$$